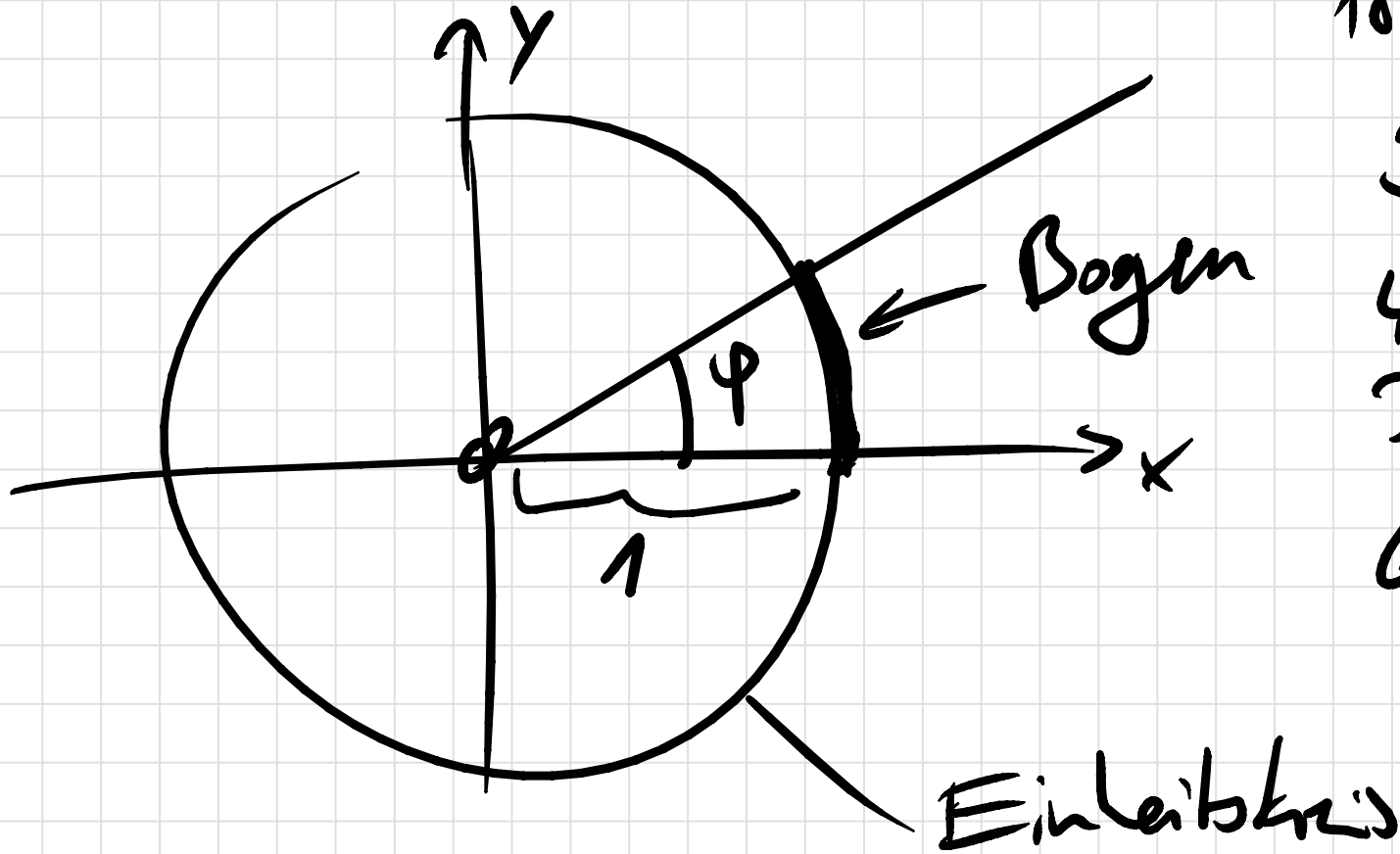


# Bogenmaß

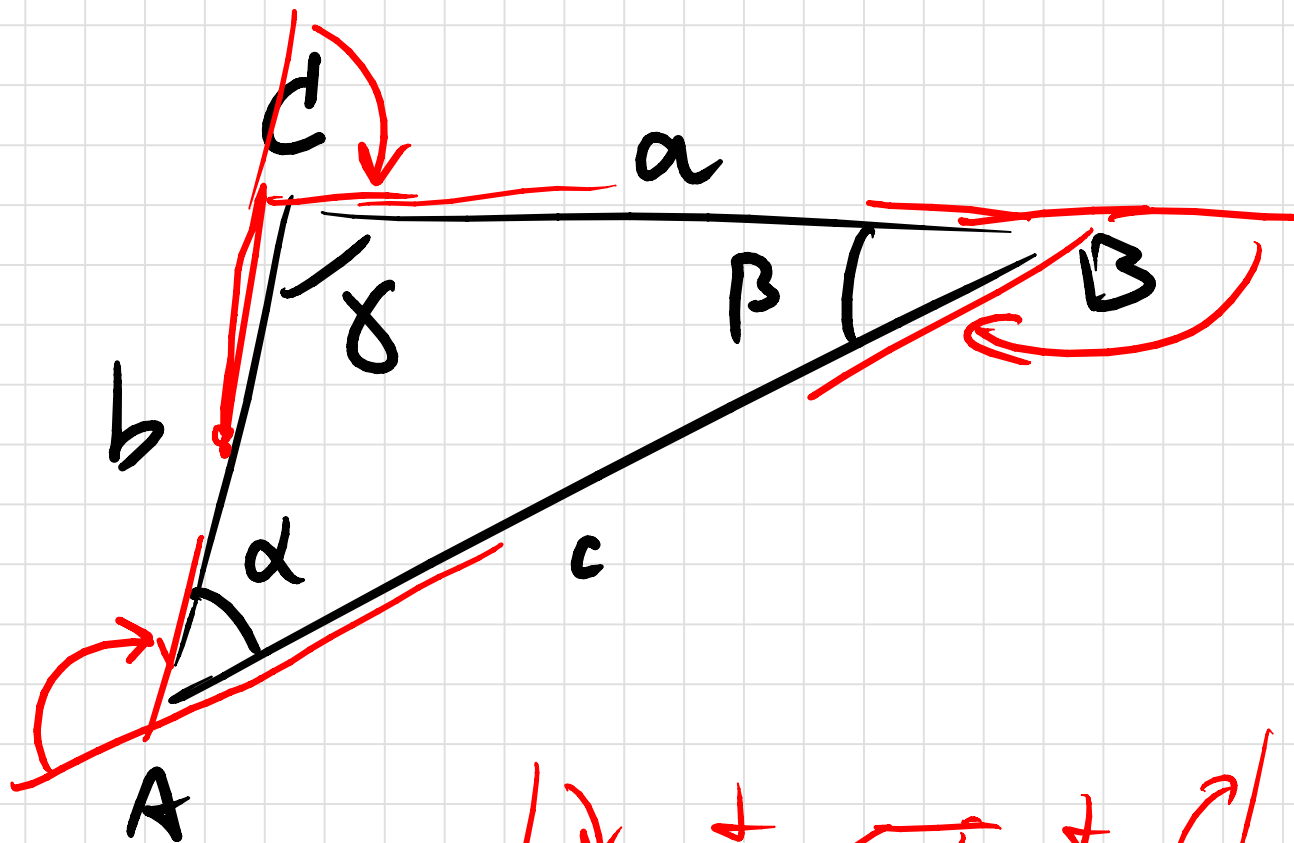


| $^{\circ}$    | rad             |
|---------------|-----------------|
| $360^{\circ}$ | $2\pi$          |
| $180^{\circ}$ | $\pi$           |
| $90^{\circ}$  | $\frac{\pi}{2}$ |
| $45^{\circ}$  | $\frac{\pi}{4}$ |
| $30^{\circ}$  | $\frac{\pi}{6}$ |
| $60^{\circ}$  | $\frac{\pi}{3}$ |
| $0^{\circ}$   | $0$             |

Winkel im Bogenmaß

$$= \frac{\pi}{180^\circ} \cdot \text{Winkel in Grad}$$

|                | Winkel grad (°) | Rad     | gon              |
|----------------|-----------------|---------|------------------|
|                | $360^\circ$     | $2\pi$  | $400\text{ gon}$ |
| rechter Winkel | $90^\circ$      | $\pi/2$ | $100\text{ gon}$ |

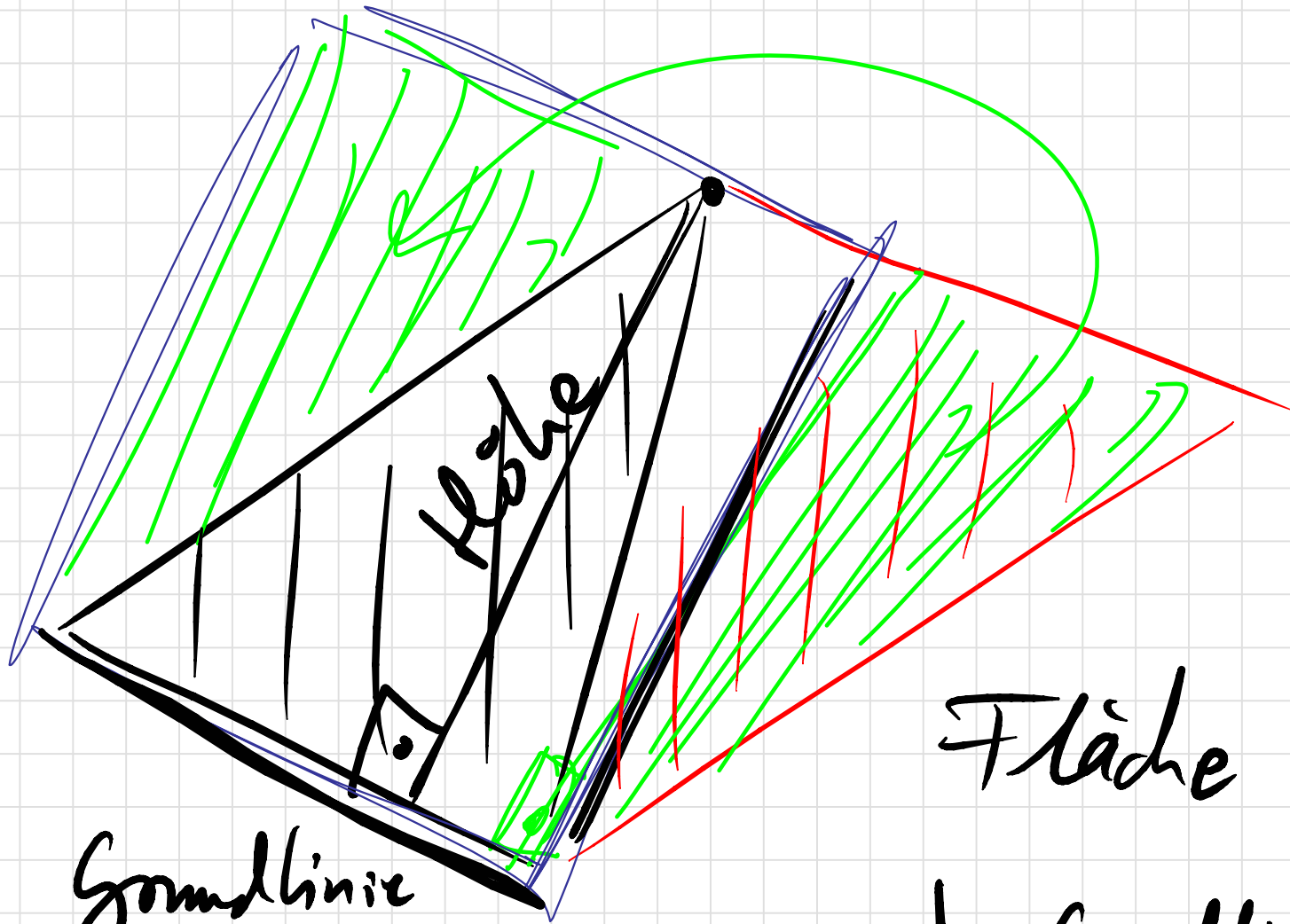


$$\begin{array}{c}
 \downarrow + \curvearrowright + \curvearrowleft = 360^\circ \\
 | \quad | \quad | \\
 180^\circ - \gamma \quad 180^\circ - \beta \quad 180^\circ - \alpha
 \end{array}$$

}

$$\cancel{360^\circ} + 180^\circ - \alpha - \beta - \gamma = \cancel{360^\circ}$$

$$\Rightarrow \alpha + \beta + \gamma = 180^\circ$$

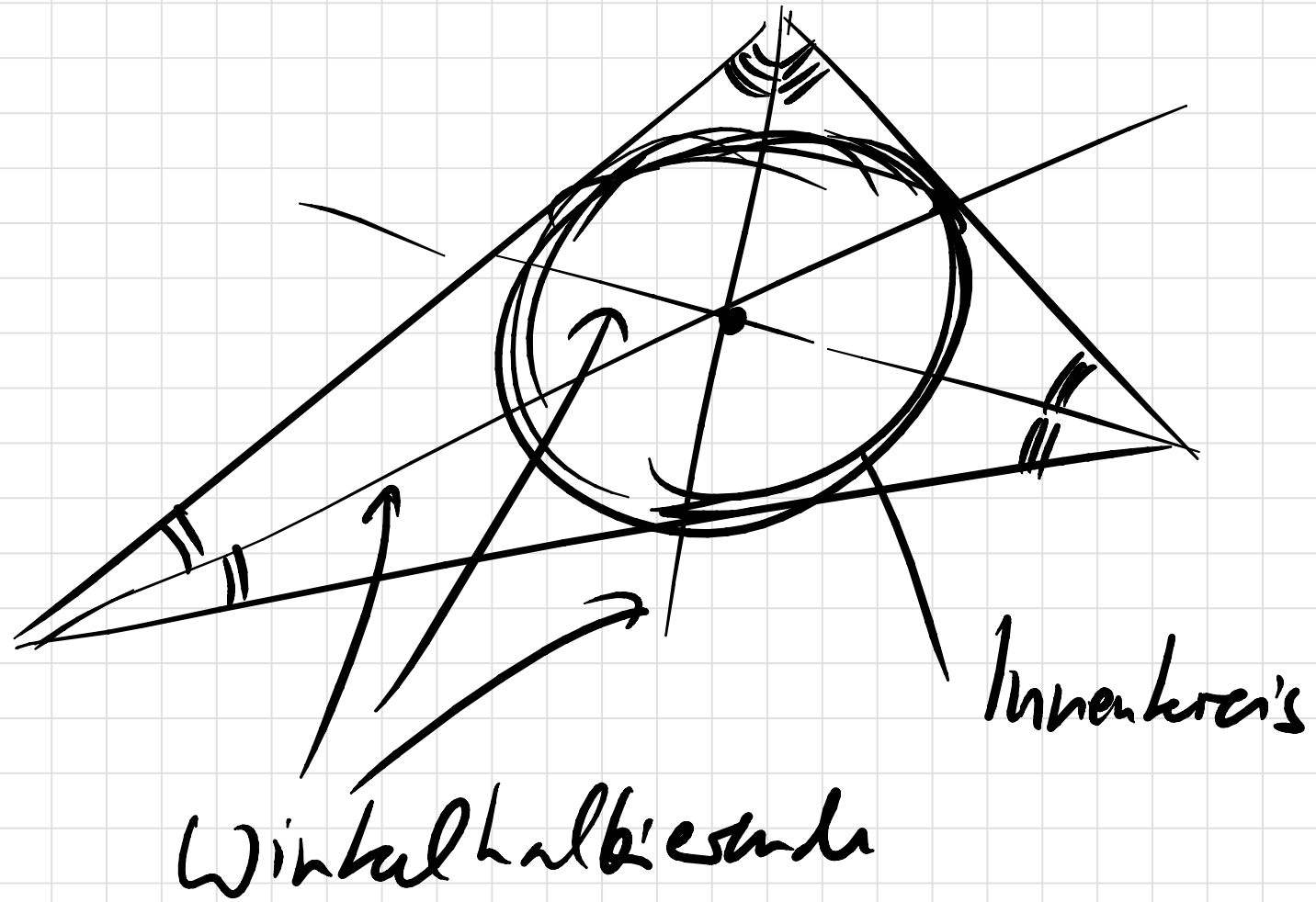


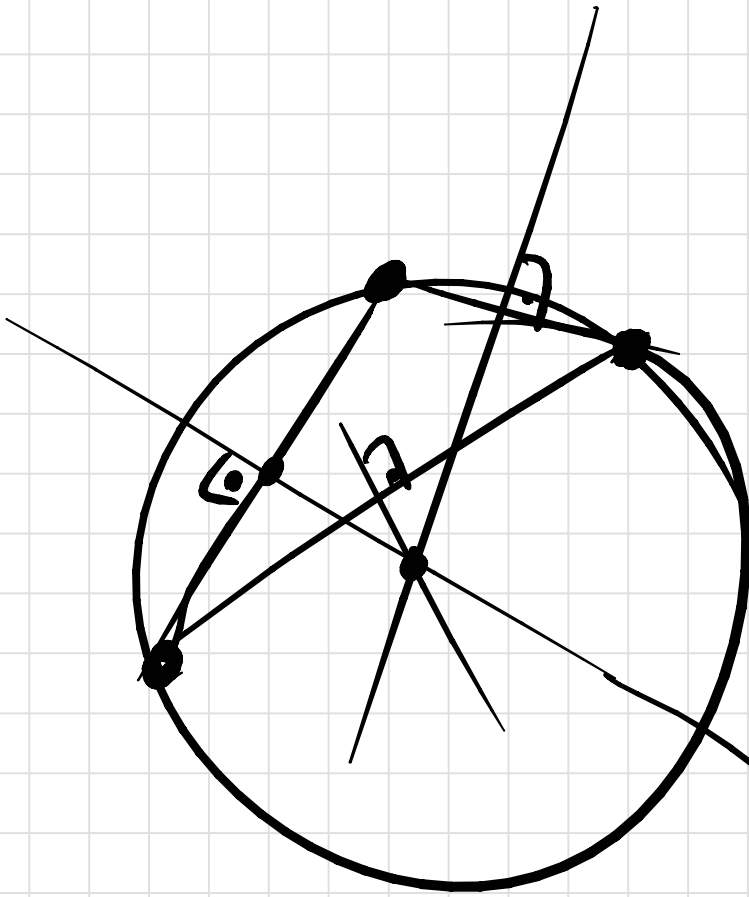
Grundlinie

Höhe

Fläche  $\triangle$

$$= \frac{1}{2} \text{ Grundlinie} \cdot \text{Höhe}$$

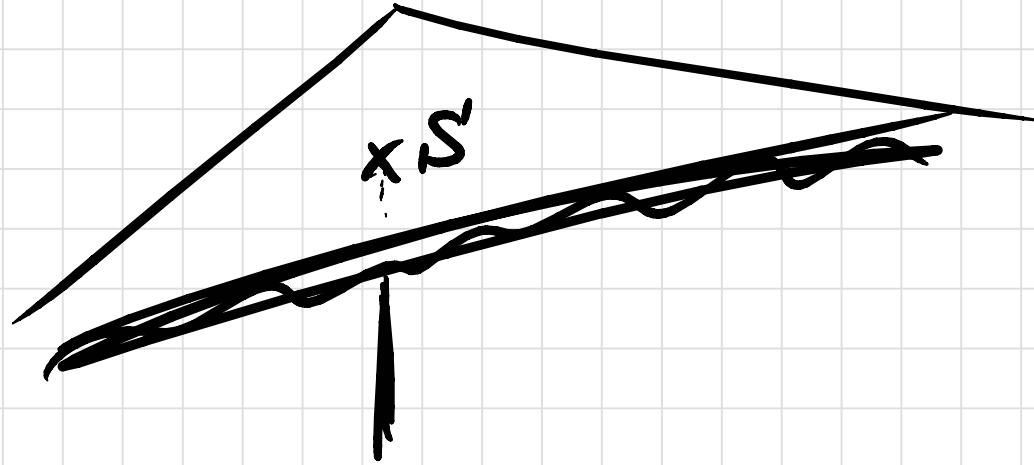


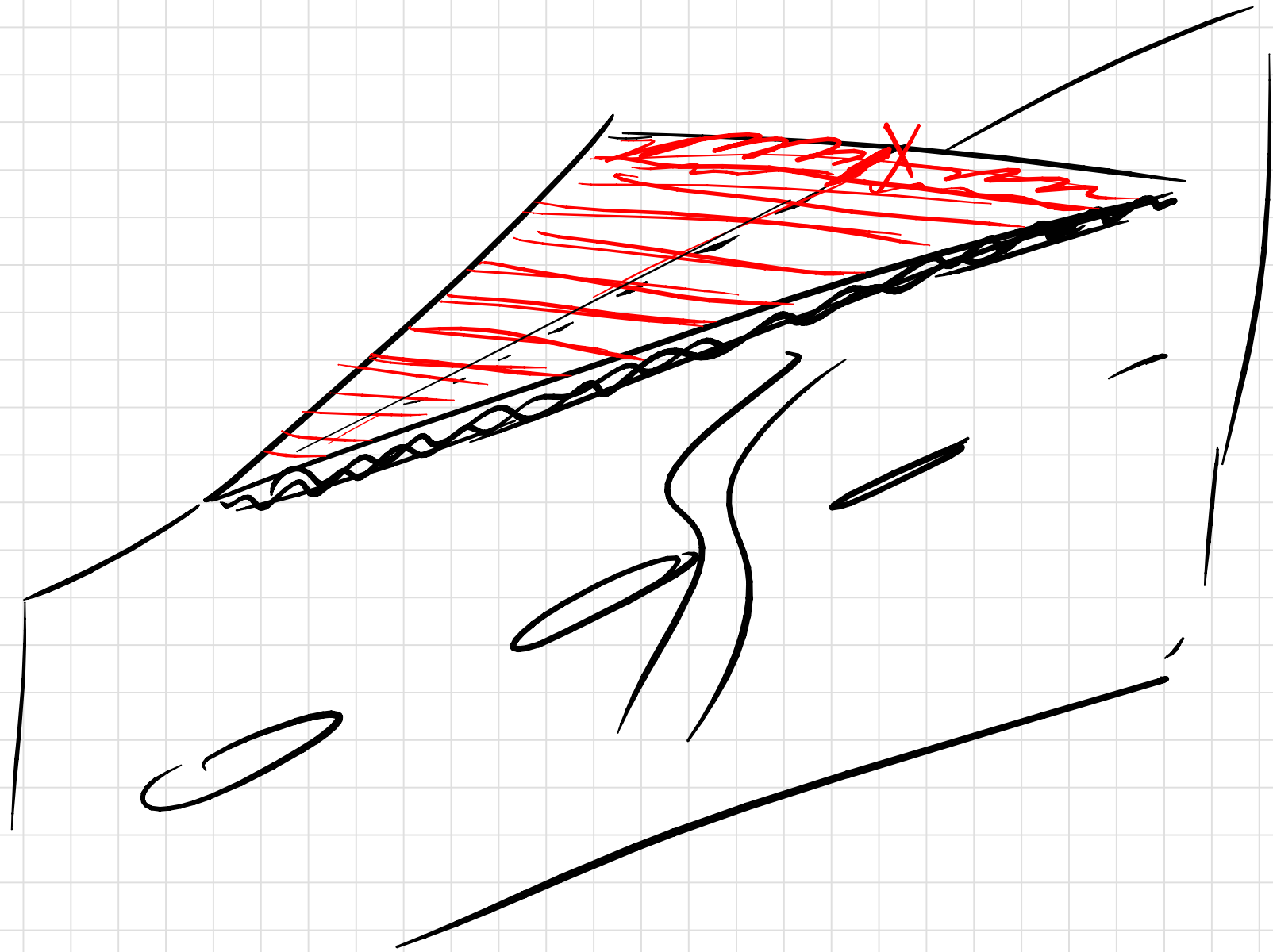


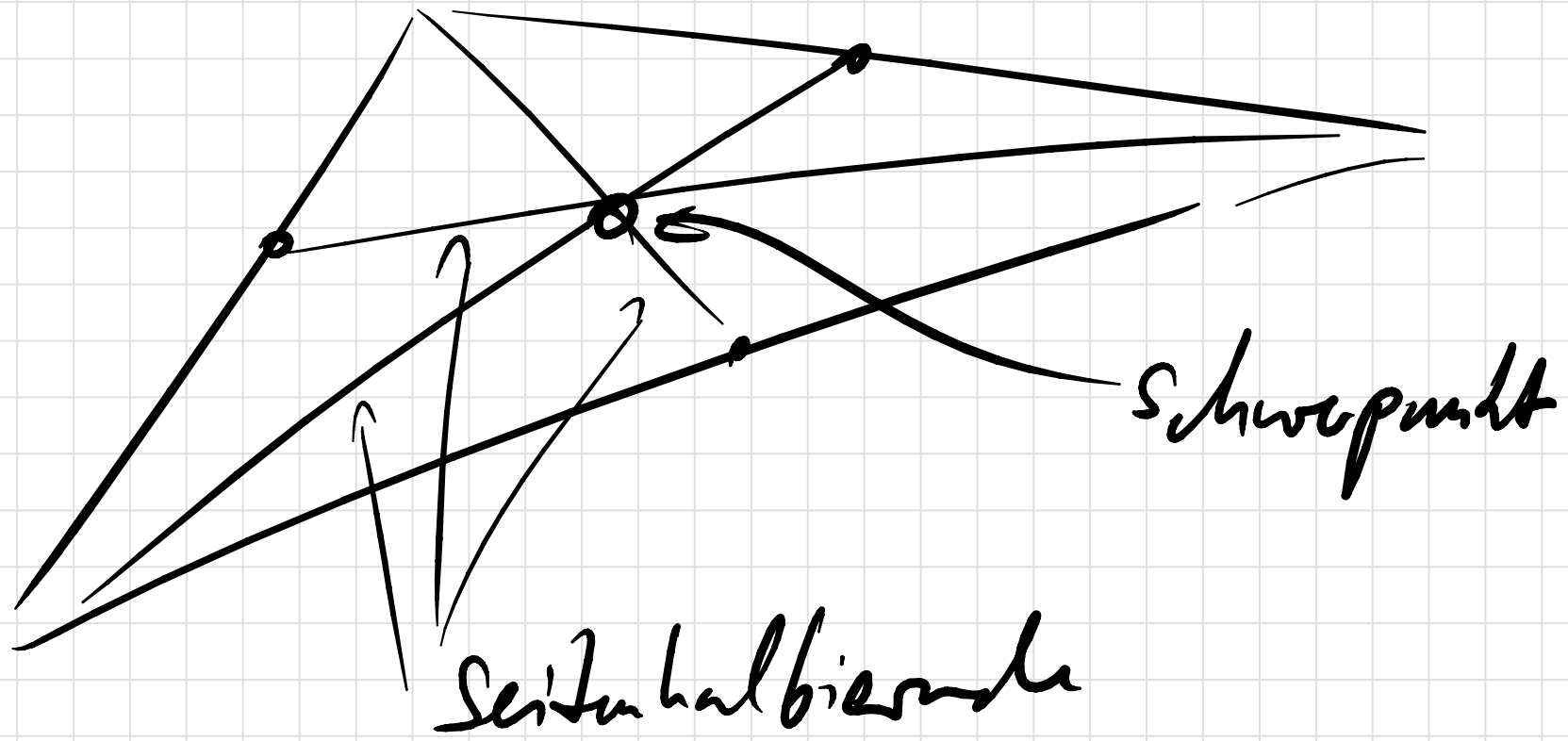
Äußere Kreis

Mittelpunkt

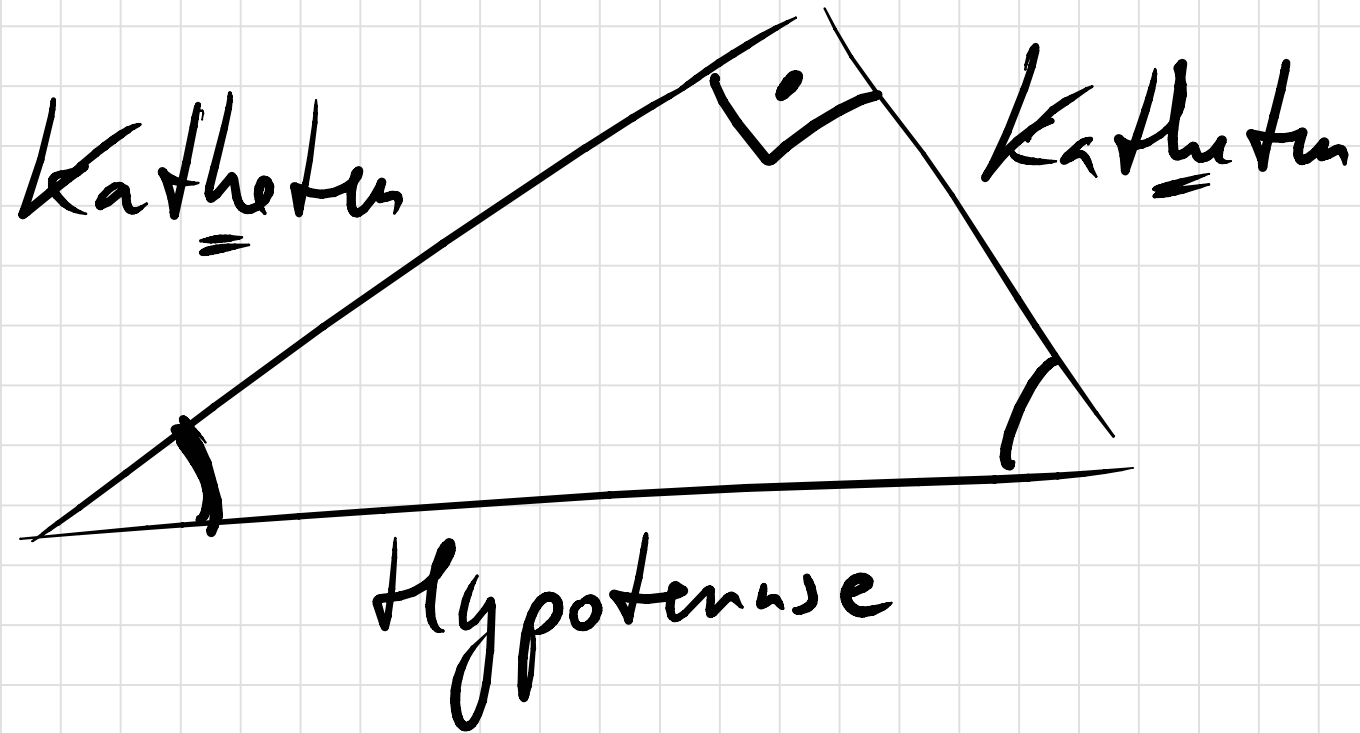




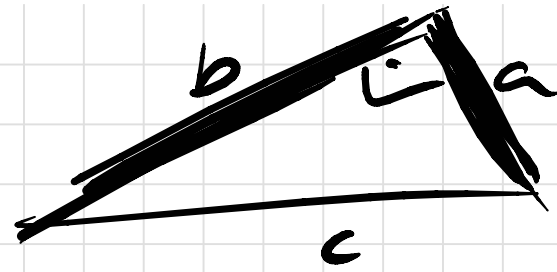
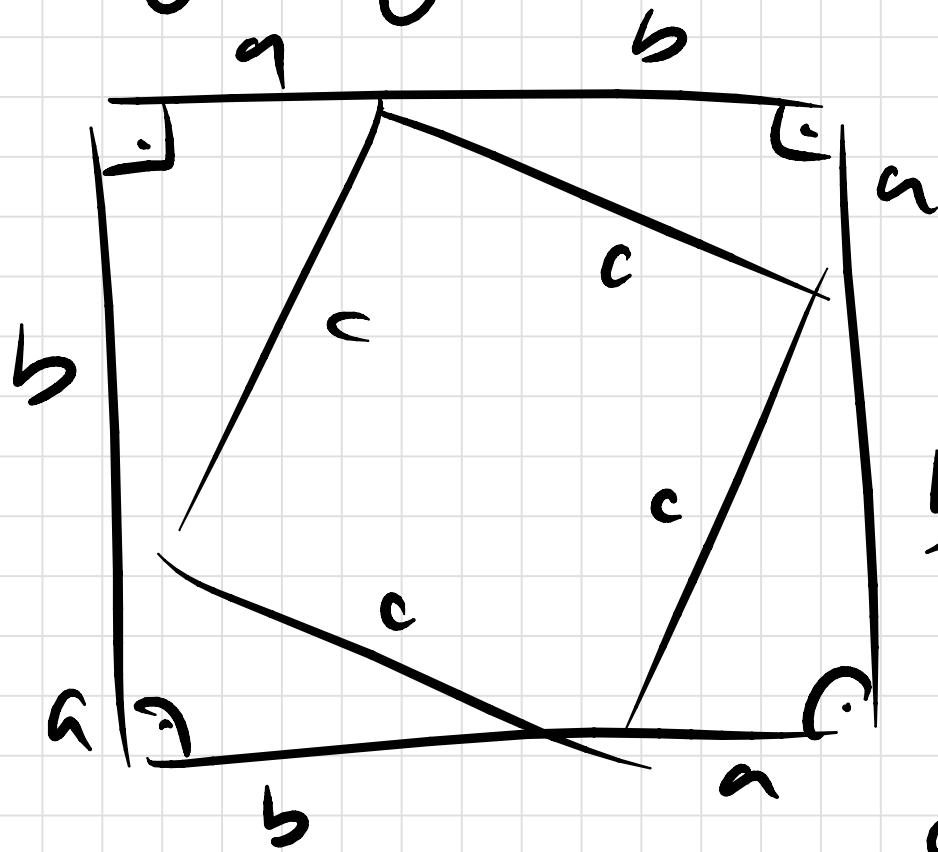




Rechtwinkliges Dreieck



# Pythagoras



Fläche =

$$(a+b)^2$$

$$= c^2 + 4 \cdot \frac{1}{2} ab$$

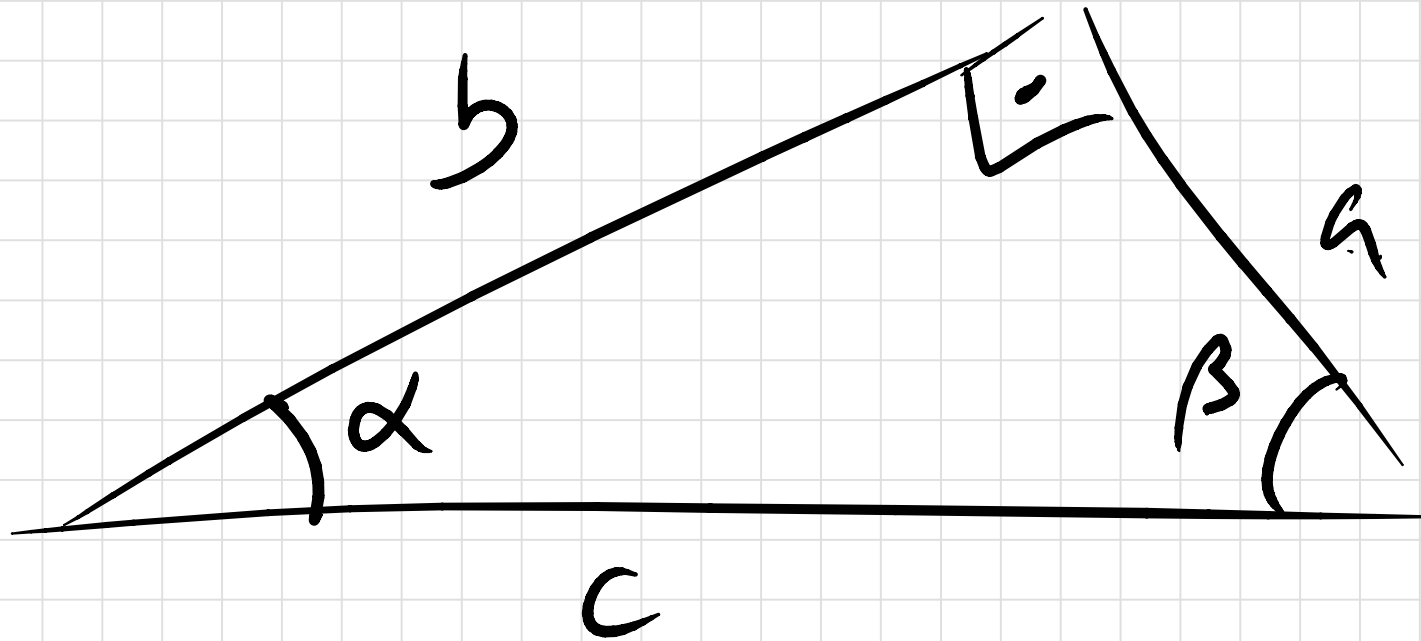
Bzw.:

$$a^2 + \cancel{2ab} + b^2$$

$$= c^2 + \cancel{2ab}$$

|| -2ab

# Sinus & Cosinus



$$\sin(\alpha) = \frac{a}{c} = \frac{GK_{\alpha}}{HY} = \frac{AK_{\beta}}{HY} = \cos(\beta)$$

$$\cos(\alpha) = \frac{b}{c} = \frac{Ak_\alpha}{Hy} = \frac{Gk_\beta}{Hy} = \sin(\beta)$$

$$\tan(\alpha) = \frac{a}{b} = \frac{Gk_\alpha}{Ak_\alpha} = \frac{Ak_\beta}{Gk_\beta} = \cot(\beta)$$

$$\cot(\alpha) = \frac{b}{a} = \frac{Ak_\alpha}{Gk_\alpha} = \frac{1}{\tan(\alpha)}$$

$$= \dots = \tan(\beta) = \frac{1}{\cot(\beta)}$$

$$\tan(\alpha) = \frac{a}{b} = \frac{\frac{a}{c}}{\frac{b}{c}} = \frac{\sin(\alpha)}{\cos(\alpha)}$$

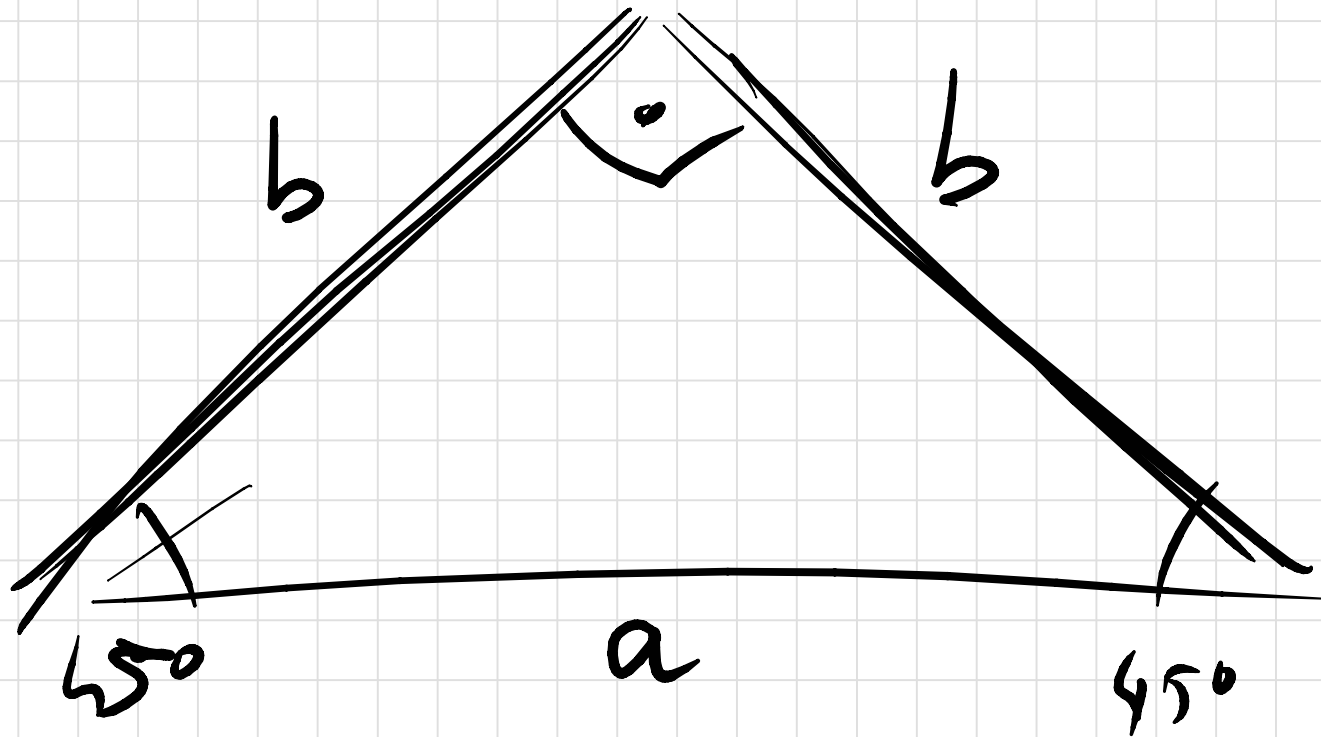
Pythagoras:

$$a^2 + b^2 = c^2$$

$$\begin{aligned} \sin^2(\alpha) + \cos^2(\alpha) &= \frac{a^2}{c^2} + \frac{b^2}{c^2} = \frac{a^2 + b^2}{c^2} \\ &= \frac{c^2}{c^2} = 1. \end{aligned}$$

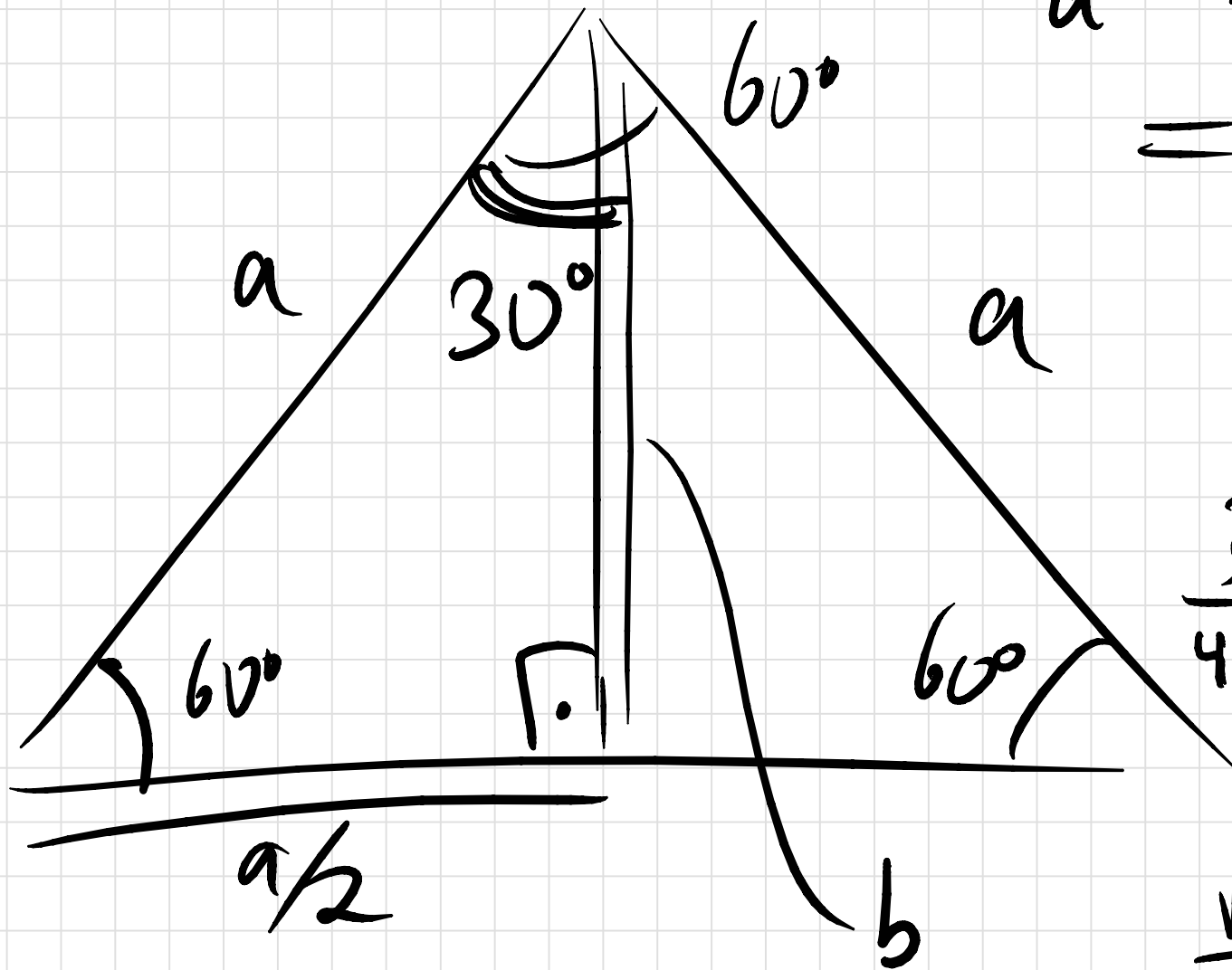


| $\varphi$          | $\sin(\varphi)$ | $\cos(\varphi)$ | $\tan(\varphi)$ | $\cot(\varphi)$ |
|--------------------|-----------------|-----------------|-----------------|-----------------|
| $0^\circ = 0$      | 0               | 1               | 0               | n.d.            |
| $30^\circ = \pi/6$ | $1/2$           | $\sqrt{3}/2$    | $1/\sqrt{3}$    | $\sqrt{3}$      |
| $45^\circ = \pi/4$ | $1/\sqrt{2}$    | $1/\sqrt{2}$    | 1               | 1               |
| $60^\circ = \pi/3$ | $\sqrt{3}/2$    | $1/2$           | $\sqrt{3}$      | $1/\sqrt{3}$    |
| $90^\circ = \pi/2$ | 1               | 0               | n.d.            | 0               |



$$\text{Pythagoras: } b^2 + b^2 = a^2$$
$$\Rightarrow 2b^2 = a^2 \Rightarrow \sqrt{2} b = a$$

$$\sin(45^\circ) = \frac{b}{a} = \frac{1}{\sqrt{2}} = \frac{1}{\sqrt{2}}$$



$$a^2 = b^2 + \left(\frac{a}{2}\right)^2$$

$$= b^2 + \frac{a^2}{4}$$

$$\Downarrow$$

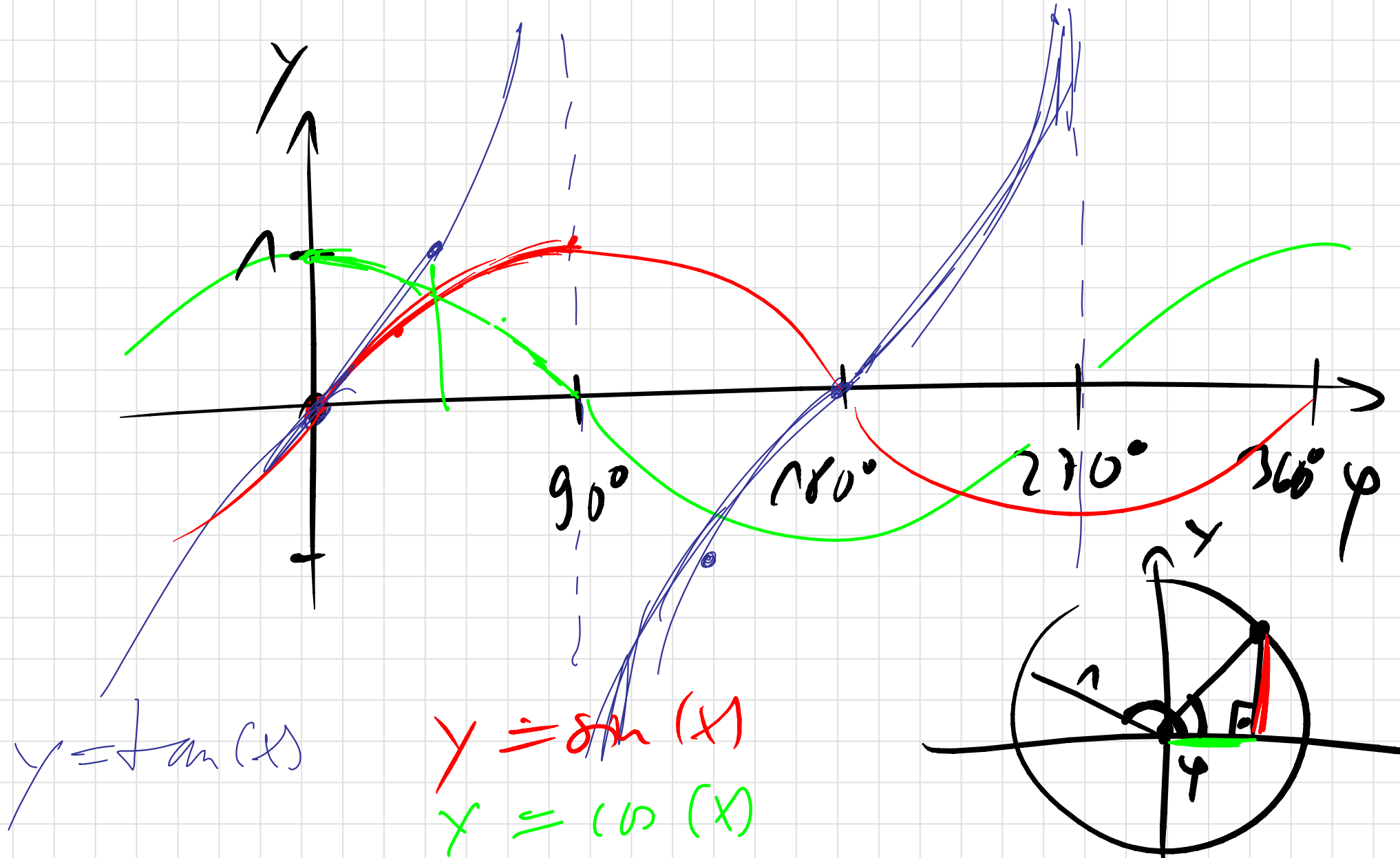
$$\frac{3}{4}a^2 = b^2$$

$$\Downarrow$$

$$\frac{\sqrt{3}}{2}a = b$$

$$\sin(60^\circ) = \frac{b}{a} = \frac{\frac{\sqrt{3}}{2}a}{a} = \frac{\sqrt{3}}{2}$$

$$\cos(60^\circ) = \frac{a/2}{a} = \frac{1/2 a}{a} = \frac{1}{2}$$



# Addition's theorem

$$\sin(\alpha + \beta) = \sin(\alpha) \cos(\beta) + \cos(\alpha) \sin(\beta)$$

---

$$\sin(x + 42^\circ)$$

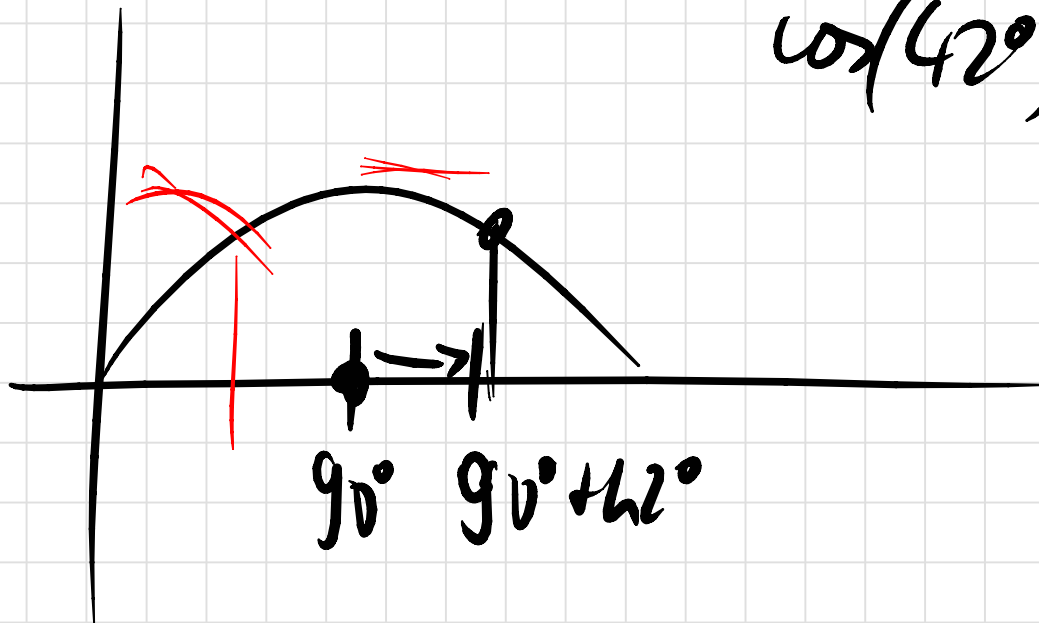
$$= A \sin(x) + B \cos(x)$$

*cos(42°)* (with arrow pointing to A)  
*sin(42°)* (with arrow pointing to B)

mit  $A = ?$ ,  $B = ?$

$$x = 0^\circ \Rightarrow \sin(42^\circ) = \frac{A \sin(0^\circ) + B \cos(0^\circ)}{1} = B$$

$$x = 90^\circ \Rightarrow \underbrace{\sin(90^\circ + 42^\circ)}_{\cos(42^\circ)} = A \overset{\uparrow}{\sin(90^\circ)} + B \frac{\cos(90^\circ)}{0} = A$$





$$\cos(\alpha + \beta) = \cos(\alpha)\cos(\beta) - \sin(\alpha)\sin(\beta)$$

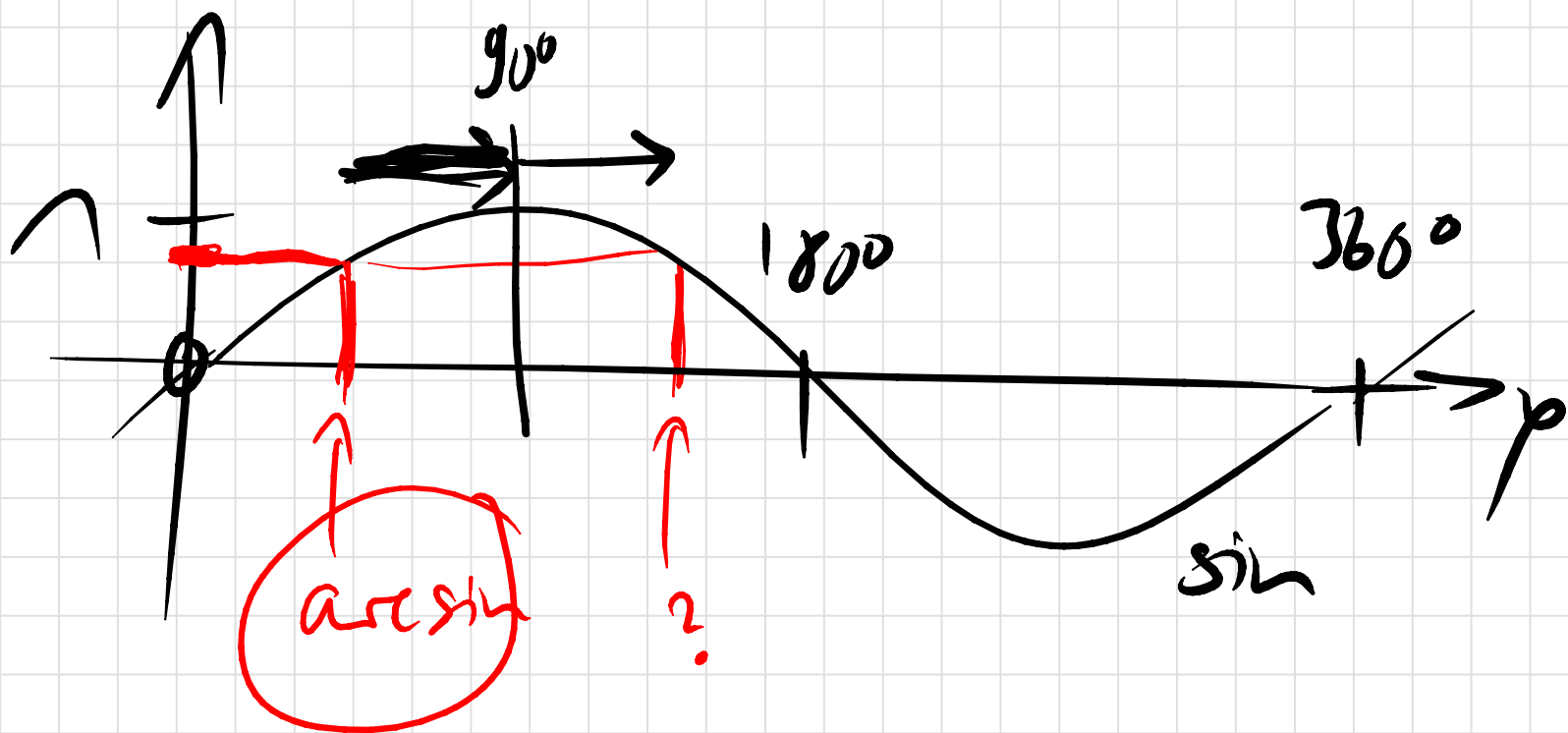
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$$e^{j\varphi} = \cos \varphi + j \sin \varphi$$

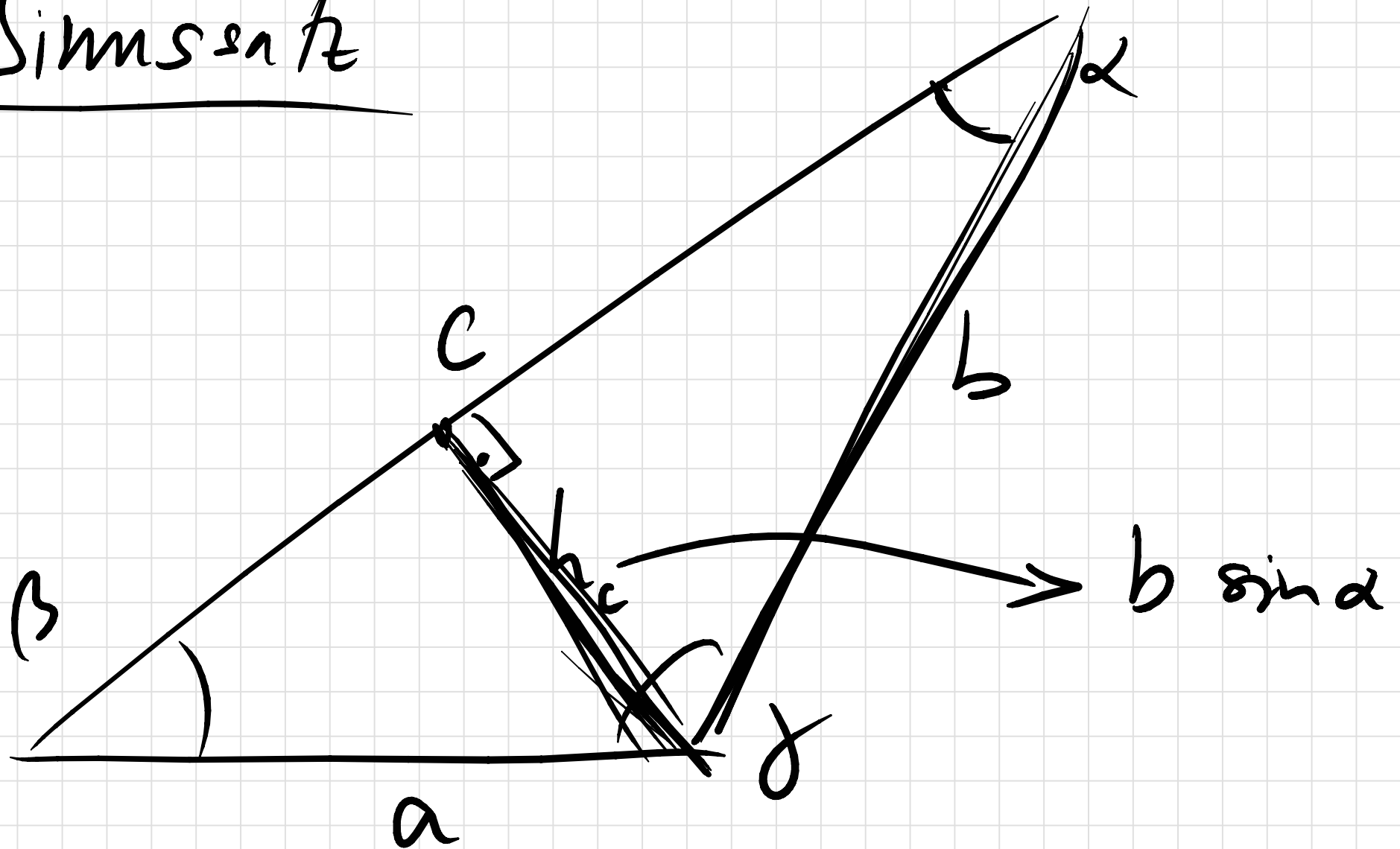
# Arcusfunktionen

$$\sin(\varphi) = 0,93 \quad | \text{ arcsin}$$

$$\varphi = \arcsin(0,93)$$



# Sinussatz



$$\text{Fläche} = \frac{1}{2} a \cdot h_a = \frac{1}{2} \cdot a \cdot c \cdot \sin \beta$$

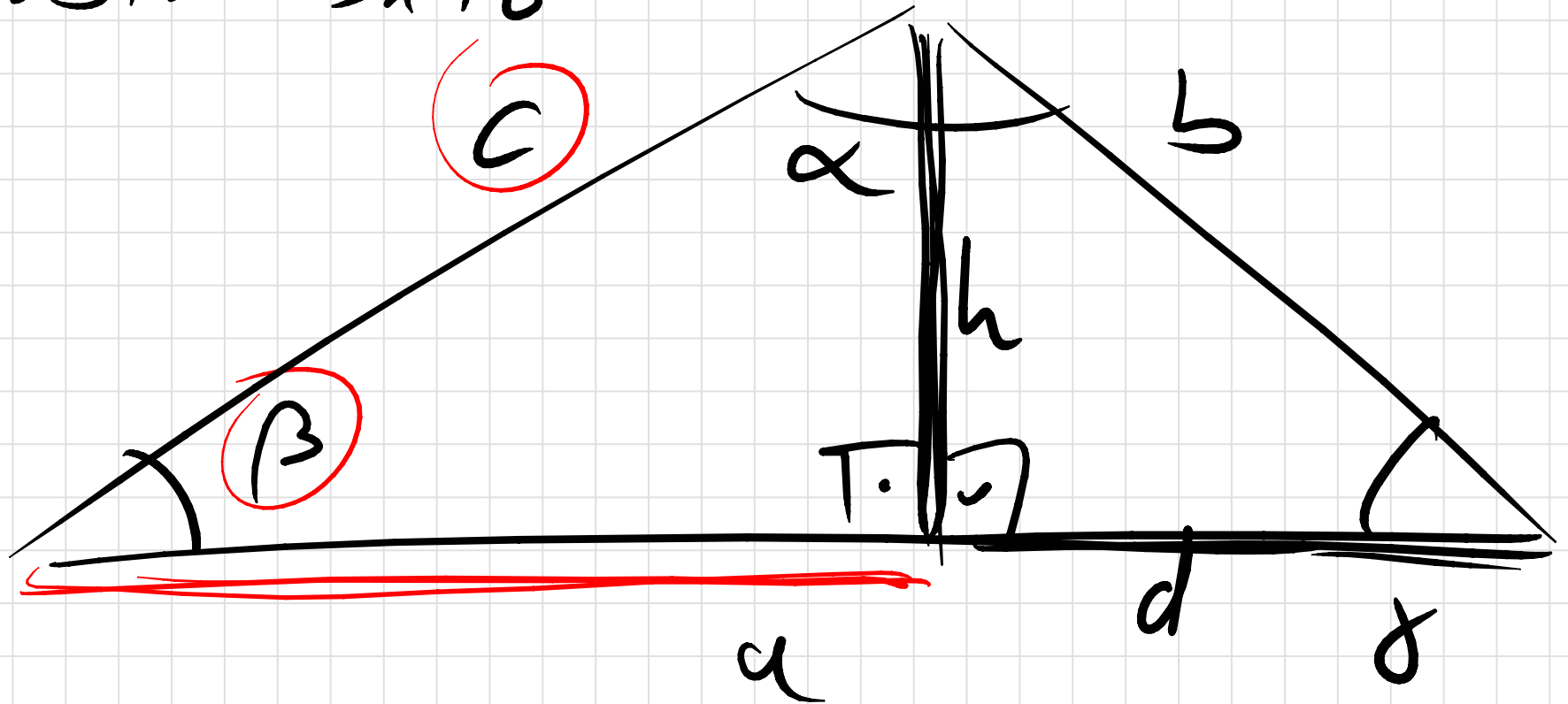
$$= \frac{1}{2} c \cdot h_c = \frac{1}{2} c \cdot b \sin \alpha$$

$$\Rightarrow \cancel{\frac{1}{2}} a \cancel{c} \sin \beta = \cancel{\frac{1}{2}} c \cancel{b} \sin \alpha$$

$$\Rightarrow a \sin \beta = b \sin \alpha \quad || :a \quad :b$$

$$\Rightarrow \frac{\sin \beta}{b} = \frac{\sin \alpha}{a} = \frac{\sin \alpha}{c}$$

Castellum SA AB



$$b^2 = d^2 + h^2$$

$$h = c \sin \beta$$

$$d = a - c \cos \beta$$

$$\hookrightarrow = (a - c \cos \beta)^2 + (c \sin \beta)^2$$

$$= a^2 - 2ac \cos \beta + c^2 \cos^2 \beta$$

$$+ c^2 \sin^2 \beta$$

$$= a^2 - 2ac \cos \beta + c^2 (\cos^2 \beta + \sin^2 \beta)$$

$$= a^2 + c^2 - 2ac \cos \beta \quad \uparrow$$

$$a^2 = b^2 + c^2 - 2bc \cos \alpha$$

$$c^2 = a^2 + b^2 - 2ab \cos \gamma$$

A  
B  
C  
Δ  
E  
Z

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Alpha  
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Gamma  
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Omicron  
Pi  
Sigma  
Tau  
Upsilon  
Phi  
Psi  
Omega

